

# Multiscale Analysis Wavelet Coefficients with Smoothness-Constrained Mean Noisy Configuration Algorithm

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Wavelet theory has played a particularly important role in multiscale analysis due to the fact that the basis functions are well suited to analyze local scale phenomena. This research also endows wavelets with a remarkable property for denoising in a wavelet based framework. In this paper, we show that effective noise uppression may be achieved by wavelet shrinkage.

## Introduction

Given the noisy wavelet coefficients, the true wavelet coefficients plus a noise term, and assuming that one has knowledge of the true wavelet coefficients, an ideal filter sets a noisy coefficient to zero if the noise variance is greater than the square of the true wavelet coefficient; otherwise the noisy coefficient is kept. In this way, the mean square error of this ideal estimator is the minimum of and the square of the coefficient. Under the assumption of i.i.d. normal noise, it can show that a soft thresholding estimator achieves times the risk of this ideal estimator. in this paper, we have taken a mini-max approach to characterize the signal, and proved, by setting a threshold, that the estimation risk is close to the minimax risk, then given an alternative derivation for this threshold, using Minimum Description Length criterion and the assumption of normally distributed noise. The threshold increases due to the tail of the Gaussian distribution, which tends to generate larger noise coefficients. To refine the threshold, a SureShrink [1-2] procedure is proposed. This non-linear filter

would be optimal in the sense of recovering the smoothness of the true underlying signal. A crucial step for realizing such a smoothness-constrained filter is to identify the singularities of the true signal. We tackle this problem with the theory of curve evolution, which is inherently geometric in nature, and widely used in computer vision and image processing. SureShrink calculates thresholds by the principle of minimizing the Stein unbiased estimate of risk for threshold estimates. Sure-Shrink is also based on the assumption of i.i.d. normal noise. For non-Gaussian type of noise, Ref. [2-5], studied the choice of thresholds by having recourse to asymptotics.

## Methods and Materials

We know the statistics of the noise to determine an adequate threshold. This makes the algorithm less flexible and less adaptive to different scenarios which can result in an even worse reconstruction. Compensation for the lack of a prior knowledge of the noise statistics may be handled by adopting the mini-max principle upon deriving the worst case noise distribution. To characterize the singular structures, exponents [4] provide a point wise measure of a function over a time interval. Due to the pioneering work by [5], it can be shown that a local signal singularity of a function is characterized by the decay of its wavelet transform amplitude across scales. In this paper we first reinterpret the demising problem as one of having to adjust the point wise smoothness of noisy data, and propose a novel non-linear

estimator as a result. Figure 1, original image and edge extraction from image. The key idea is to separate out the signal portion from its noisy data to preserve the original smoothness property of the underlying signal, while the remaining noisy data admits the same exponents as the noise. The basic idea is that a planar curve deforms in the direction of its Euclidean normal, with a speed equal to its curvature. The noise riding on the signal has relatively higher curvatures in comparison to the underlying signal. It thus tends to be smoothed much faster than the latter. This disparity in evolution speed is key to preserving the true features of the signal. With the knowledge of the singularities, we proceed to generate a multistage curvature mask to filter the wavelet transform of the noisy data. Specifically, we prove that filtering the transform by a curvature mask is equivalent to keeping the pointwise exponent of the noisy data at singular points, and lifting its smoothness. It is, generally not possible to have enough information to define this prior probability distribution for a signal set with complex structure. To overcome this difficulty, one may call upon a minimax framework that applies a simpler model which constrains signals in a prior-set. The goal is to then find an optimal operator which minimizes the maximum risk over where the maximum risk is given by. Except for a few special cases, minimax optimal operators are highly nonlinear and difficult to find for real world applications. More often than not, one settles for a suboptimal estimator. The thresholding estimator in an orthonormal wavelet basis

proposed has a suboptimal risk for the set of piecewise smooth signals, where the observation length is the min risk.

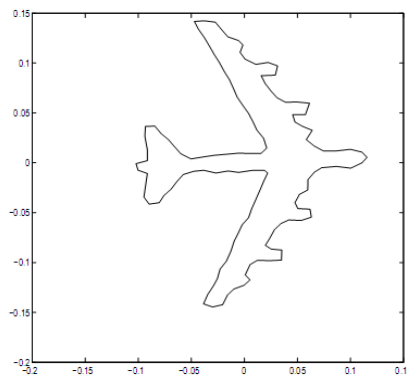


**Figure 1.** Original image and edge points extraction from image

## Results and Discussion

To find and minimize the estimator data coefficients are sorted in decreasing amplitude order with operations. The coefficient of rank index such that. We must choose increasing manner. It is therefore sufficient to compare the possible values, to find that requires operations if we progressively re-compute. The calculation is thus performed with operations. Although the estimator is unbiased, its variance may induce errors due to the noise energy, especially when it must impose in order to remove all the noise. We estimate and compare this value with a minimum energy. The resulting threshold is a signal set and the minimax risk of a soft thresholding obtained by optimizing the choice depending. It is proved that the threshold computed empirically yields a nearly minimax risk. It demonstrates the estimation result of with a soft threshold estimator with the threshold. It generally relied on the assumption of normally distributed perturbations. In practice, this assumption is often violated and sometimes, even prior information of probability distribution of the noise process is not available. To relax this assumption, we propose a novel non-linear filtering technique. The key idea is to project a noisy signal onto a wavelet domain and to suppress wavelet coefficients by a mask derived from curvature extreme in its scale space representation. For a piecewise smooth signal, it can be shown that filtering by this curvature mask is equivalent to preserving the signal point wise exponents at the singular points and lifting its

smoothness at all the remaining points, maiming points. In addition, residual data admits the same exponents as the noise except at the singular points of the signal. We introduce the concept of exponent and. We formally define the smoothness-constrained filter, propose its implementation and verify its properties. Some numerical results appear in characterize singular structures, it is necessary to precisely quantify the local regularity of a signal. Spaces and exponent provide a uniform regularity measurement over time intervals, as well as at a particular point. It is said to belong to global space if and only if for any there exists a positive constant and a polynomial denotes the largest integer, is said to belong to a pointwise space only if there exists a positive constant and a polynomial such that at point if there exists a polynomial degree and satisfies, the moment property of a wavelet function is crucial to measure the local regularity of a signal. If a wavelet has moments, i.e. it can be shown that the wavelet transformation is actually a multiscale differential operator of order. This nice property relates the differentiability with its wavelet transform decay at fine scales. Due to the pioneering, it can be shown that a local signal singularity is characterized by the decay of its wavelet transform amplitude across scales. Wavelet moments denotes its wavelet transform. Figure 2 Estimated mean configuration of airplane. A signal is contaminated by the addition of a noise. This noise is modeled by the realization of a zero mean random process.



**Figure 2.** Estimated mean configuration of airplane

## Conclusion

In this paper, we propose a novel nonlinear filtering technique. we assume that a prior knowledge about point wise smoothness measure of the signal is known or can be extracted. However, this smoothness property of the signal is corrupted by additive noise, which in general has a uniform exponent. The signal is estimated by transforming the noisy observation with a decision operator, which is given by statistical approach usually assumes the knowledge of at least the probability distribution of the noise and maybe a prior distribution of the signal. ■

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